

Area finding

1) find area enclosed bet^w $y=x^2$ & $y=x+6$

Maxima, Minima & Increasing, decreasing

- 1) Intervals on which $f(x) = 2x^3 + 3x^2 - 36x$ is increasing and is decreasing.
- 2) State Extreme value theorem.
- 3) Find absolute maximum & minimum values of, $f(x) = 2x^3 - 15x^2 + 36x$ on $[1, 5]$ & determine where the value occurs.
- 4) Find maximum & minimum of:
 - i) $f(x) = 2x^3 + 3x^2 - 12x, [-3, 2]$
 - ii) $f(x) = 6x^{4/3} - 3x^{1/3}, [-1, 1]$
 - iii) $f(x) = 2x^3 - 15x^2 + 36x; [1, 5]$
 - iv) $f(x) = 4x^2 - 12x + 10; [1, 2]$
 - v) $f(x) = 8x - x^2$
 - vi) $f(x) = \frac{3x}{\sqrt{4x^2 + 1}}$
 - vii) $f(x) = 1 + |9 - x^2|; [-5, 1]$
 - viii) $f(x) = |6 - 4x|; [-3, 3]$

Multiple Integration

1) $\int_0^2 \int_{-x}^{x^2} y^2 x \, dy \, dx$

2) $\int_0^{\pi/3} \int_0^{\cos y} x \sin y \, dx \, dy$

3) Evaluate $\iint_R xy \, dA$ over the rectangle R enclosed between $y = \frac{x}{2}$, $y = \sqrt{x}$, $x = 2$ and $x = 4$

4) $\iint_R (2x - y^2) \, dA$ over the triangular region R enclosed by the lines $y = x + 1$, $y = -x + 1$, $y = x + 1$ and $y = 3$

5) Evaluate $\iiint_G 12xy^2z^3 \, dV$ over the rectangle box G defined by the

inequalities $-1 \leq x \leq 2$, $0 \leq y \leq 3$, $0 \leq z \leq 2$

6) Let G be the wedge in the first octant that is cut from the cylinder solid $y^2 - z^2 \leq 1$ by the plane $y = x$ and $x = 0$, Evaluate $\iiint_G z \, dV$

7) Use a triple integral to find the volume of the solid within the cylinder $x^2 + y^2 = 9$, and between the planes $z = 1$ and $x + z = 5$.

8) $\int_{-1}^2 \int_0^3 \int_0^2 12xy^2z^3 \, dz \, dy \, dx$

Partial Differentiation

~~(i) $F(x) =$~~ i) $F(x, y) = x^3 + y^3$

ii) $F(x, y) = 3x^2 + 2xy + 5y^2$

iii) $F(x, y) = 9x^3 + 5x^2y + 9y^2x + 3y^2$

iv) $F(x, y) = 10x^4 + 5y^4$

v) $F(x, y, z) = 3x^3 + 3x^2yz + 3xy^2z + 3y^3 + 3z^2yx + 3z^3$

vi) $F(x, y, z) = 4x^2y^2z + 3xy^2z^3 + 9x^3y^2z$

vii) $F(x, y) = ax^2 + 2hxy + by^2$

viii) $f(x, y) = \log \log (x^2 + y^2)$

ix) $F(x, y) = x^3 + 3x^2y + 3xy^2 + y^3$

x) Show that $f(x, y) = \ln(x^2 + y^2)$, satisfies $\frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} = 0$

xi) $F(x, y) = y^{-3/2} \tan^{-1}(x/y)$

xii) 2nd order of $F, z = e^x \cos y$

(xiii) $F(x, y) = e^{xy} \sin(4y^2)$ (xiv) $\frac{\partial^2 z}{\partial x^2}$ & $\frac{\partial^2 z}{\partial y^2}$ of $z = \sqrt{x} \cos y$

~~(xiv) $F(x, y) =$~~ (xv) $F(x, y) =$ (xvi) $\frac{\partial z}{\partial x}$ & $\frac{\partial z}{\partial y}$, $z = x^4 \sin(xy^3)$

(xvii) 2nd derivative of $z = x^2y^3 + x^4y$

Definite integration

Integration

- (1) $\int_{-1}^1 x^2 dx$ (2) $\int_{-1}^1 (2x^2 - x^3) dx$ (3) $\int_0^{\pi/2} \sin^2 x dx$ (4) $\int_0^{\pi/2} \frac{\cos^2 \theta}{1 - \sin \theta} d\theta$
- (5) $\int_2^3 2x dx$ (6) $\int_1^4 \frac{1}{x^3} dx$ (7) $\int_1^3 (4 + 3x - x^3) dx$ (8) $\int_0^1 (\sqrt{x} + \frac{1}{\sqrt{x}}) dx$
- (9) $\int_{-3}^1 (x^2 + 2) dx$ (10) $\int_{-3}^1 (5 - 2x) dx$ (11) $\int_0^2 (2x - x^2) dx$ (12) $\int_1^2 (x^2 + 2x + 5) dx$
- (13) $\int_{-2}^3 (x + 6 - x^2) dx$ (14) $\int_0^{\ln 2} e^y (1 + e^y)^{1/2} dy$ (15) $\int_1^{\sqrt{2}} \frac{1}{x^2 \sqrt{4 - x^2}} dx$
- (16) $\int_4^9 (4y^{-1/2} + 2y^{1/2} + y^{-5/2}) dy$ (17) $\int_0^2 \tan^{-1} x dx$ (18) $\int_3^{\sqrt{2}} 5x \cos(x^2) dx$

(19) $\int_0^1 (2 + x^2 - 3x^4 + x^6) dx$ (20) $\int_0^1 (x+1)(x^2-1) dx$

(21) $\int_0^1 (x^2 + x + 1) dx$ (22) $\int_0^1 (x^2 + 1) dx$

(23) $\int_0^1 x^2 dx$ (24) $\int_0^1 x dx$ (25) $\int_0^1 1 dx$

(26) $\int_0^1 \frac{1}{x} dx$ (27) $\int_0^1 \sqrt{x} dx$ (28) $\int_0^1 \frac{1}{\sqrt{x}} dx$

(29) $\int_0^1 \frac{1}{x^2} dx$ (30) $\int_0^1 \frac{1}{x^3} dx$ (31) $\int_0^1 \frac{1}{x^4} dx$

(32) $\int_0^1 \frac{1}{x^5} dx$ (33) $\int_0^1 \frac{1}{x^6} dx$ (34) $\int_0^1 \frac{1}{x^7} dx$

(35) $\int_0^1 \frac{1}{x^8} dx$ (36) $\int_0^1 \frac{1}{x^9} dx$ (37) $\int_0^1 \frac{1}{x^{10}} dx$

(38) $\int_0^1 \frac{1}{x^{11}} dx$ (39) $\int_0^1 \frac{1}{x^{12}} dx$ (40) $\int_0^1 \frac{1}{x^{13}} dx$

Gamma & Beta

$$\pi = \frac{22}{7}$$

1) Prove that $\Gamma\left(\frac{1}{2}\right) = \sqrt{\pi}$

(2) $\int_0^1 x^9 (1-x)^4 dx$ (3) $\int_0^1 x^7 (1-x)^3 dx$

(4) $\int_0^1 x^3 (1-x)^{1/2} dx$ (5) $\int_0^1 x^{3/2} (1-x)^{5/2} dx$

(6) $\int_0^{\infty} x^5 e^{-4x} dx$ (7) $\int_0^1 (1-x^3)^{-1/2} dx$

(8) $\int_0^{\pi/2} \sin^4 \theta \cos^2 \theta d\theta$ (9) $\int_0^1 x^5 (1-x)^{5/2} dx$

(10) $\int_0^{\pi/2} \sin^5 x \cos^4 x dx$ (11) $\int_0^{\pi/2} \sin^{12} x dx$ (12) $\int_0^1 x^4 (1-x)^{3/2} dx$

(13) $\int_0^{\pi/2} \sin^5 x dx$ (14) $\int_0^{\pi/2} \cos^3 x dx$ (15) $\int_1^e x^2 \ln x dx$

Integration

Definite Integration

$$(i) \int \frac{\sqrt{x^2-4}}{x} dx \quad (ii) \int \frac{1}{(\sqrt{x+1})^3} dx \quad (iii) \int \frac{x-1}{x^2+3x+2} dx$$

$$(iv) \int \frac{1}{(x+4)(x-1)} dx \quad (v) \int \sec^2 x dx \quad (vi) \int \frac{1}{x} dx$$

$$(vii) \int \frac{\cos x}{\sin^2 x} dx \quad (viii) \int \sqrt{1+\sin 2x} dx \quad (ix) \int \frac{1}{1-\sin x} dx$$

$$(10) \int 5x^3 dx \quad (11) \int \frac{2}{x} dx \quad (12) \int \frac{x^4+1}{x^2} dx \quad (13) \int \frac{(1+x)}{x} dx$$

$$(14) \int (x^2 + e^x + 2^x) dx \quad (15) \int (4x^3 + 3x^2 - 2x + 5) dx$$

$$(16) \int (1-3x)(1+x) dx \quad (17) \int (3x^{-1} + 4x^2 - 3x + 8) dx$$

$$(18) \int (8e^x - 4a^x + 3x^{-1} + \sqrt[4]{x}) dx \quad (19) \int (2x+9)^5 dx$$

$$(20) \int \sqrt{(5x+7)^3} dx \quad (21) \int (x^3+2)^3 \cdot 3x^2 dx \quad (22) \int x^2 2e^x dx$$

$$(23) \int \frac{1}{x \log_e x \log_e (\log_e x)} dx \quad (24) \int x^2 \sqrt{x-1} dx \quad (25) \int \frac{\sqrt{x^2-16}}{x} dx, x \geq 4$$

$$(26) \int y^4 \sqrt[3]{5-4y^5} dy \quad (27) \int \frac{5x-10}{x^2-3x-4} dx \quad (28) \int x^2 \ln x dx \quad (29) \int x^2 \sqrt{1+x} dx$$

$$(30) \int \frac{\sqrt{x^2-25}}{x} dx, x \geq 5 \quad (31) \int \frac{\cos \sqrt{y}}{\sqrt{y}} dy \quad (32) \int \frac{e^x}{\sqrt{1-e^{2x}}} dx$$

$$(33) \int x^2 e^{-2x} dx \quad (34) \int (x^{-3} - 3x^{3/4} + 8x^2) dx \quad (35) \int \frac{\sqrt{x^2-9}}{x}, x \geq 3$$

$$(36) \int \frac{\sqrt{\tan^{-1} x}}{1+x^2} dx \quad (37) \int \frac{t-1}{(t^2+3t+2)} dt \quad (38) \int_0^{\sqrt{\pi/2}} 9x \sin(x^2) dx$$

Limit,

(i) $\lim_{x \rightarrow 0} \left(\frac{1}{x} - \frac{1}{e^x - 1} \right)$ (ii) $\lim_{x \rightarrow 0} \frac{5x^3 - 2x^2 + 1}{3x + 5}$ (iii) $\lim_{x \rightarrow 0} (1+x)^{1/x}$

~~(iv) $\lim_{x \rightarrow \infty} \frac{1}{x}$~~

(iv) $\lim_{x \rightarrow \infty} (\sqrt{x^2 + x} - x)$ (v) $\lim_{x \rightarrow \infty} \left(\frac{x^3 - x + 7}{\sqrt{9x^4 + 1}} \right)$

(vi) $\lim_{x \rightarrow \infty} \frac{x^{-4/3}}{\sin(1/x)}$ (vii) $\lim_{x \rightarrow 0} (e^x + x)^{1/x}$

(viii) $\lim_{x \rightarrow 0} \left(\frac{x - \tan^{-1} x}{x^3} \right)$ (ix) $\lim_{x \rightarrow 1} \frac{x^3 + x^2 - 5x + 3}{x^2 - 3x + 2}$

(x) $\lim_{x \rightarrow 0} \left(\frac{1}{x} - \frac{1}{\sin x} \right)$ (xi) $\lim_{x \rightarrow \pi/4} (1 - \tan x) \sec 2x$

(xii) $\lim_{x \rightarrow 0} \left(\frac{x^2}{e^x + e^{-x} - 2} \right)$ (xiii) $\lim_{x \rightarrow \infty} \left(\sqrt[3]{\frac{3x+5}{6x-5}} \right)$

(xiv) $\lim_{x \rightarrow \infty} (\sqrt{x^2 + 3x} - x)$ (xv) $\lim_{x \rightarrow 0} x \ln x$ (xvi) $\lim_{x \rightarrow 0} \left(\frac{x - \cos 3x}{x^3} \right)$

(xvii) $\lim_{t \rightarrow 2} \left(\frac{t^3 - 3t^2 - 12t + 4}{t^3 - 4t} \right)$ (xviii) $\lim_{x \rightarrow +\infty} (\sqrt{x^4 + 5x^3} - x^3)$

(xix) $\lim_{x \rightarrow 0} \frac{1 - \cos x}{x^2}$ (xx) $\lim_{s \rightarrow \infty} \sqrt[3]{\frac{2 + 3x - 5s^2}{1 + 5^s}}$